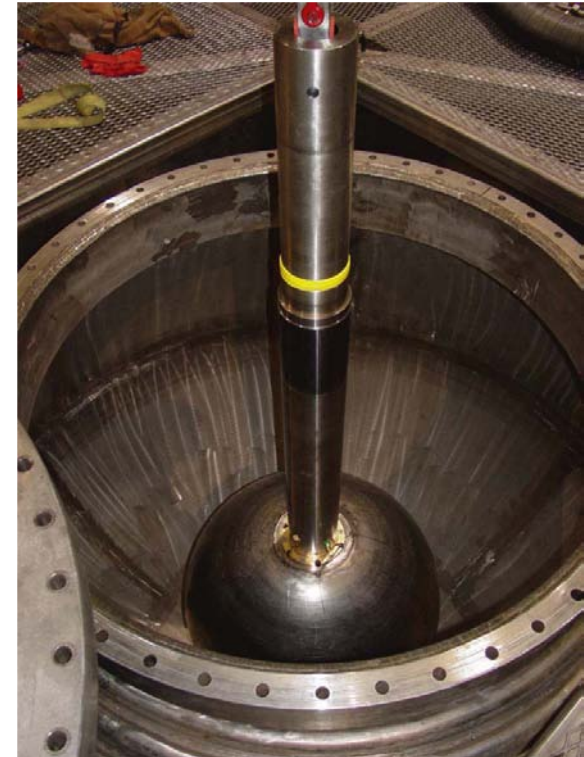
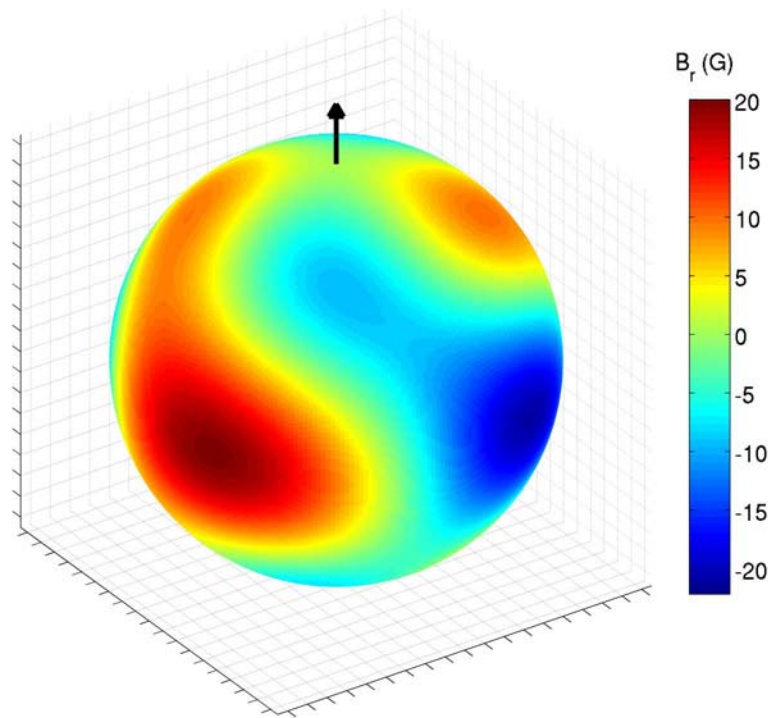


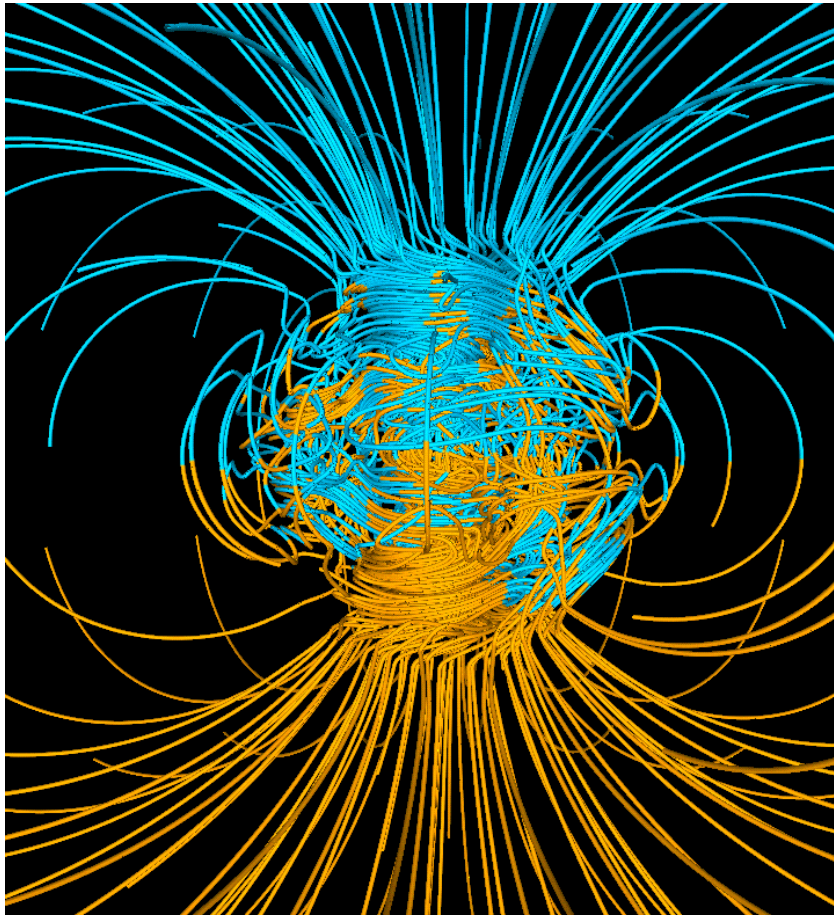
# Journey to the Center of the ERF: Planetary Cores, Accretion Disks, and "Helioseismology" in the Lab



Daniel S. Zimmerman

Funding:  
NSF EAR/Geophysics  
University of Maryland

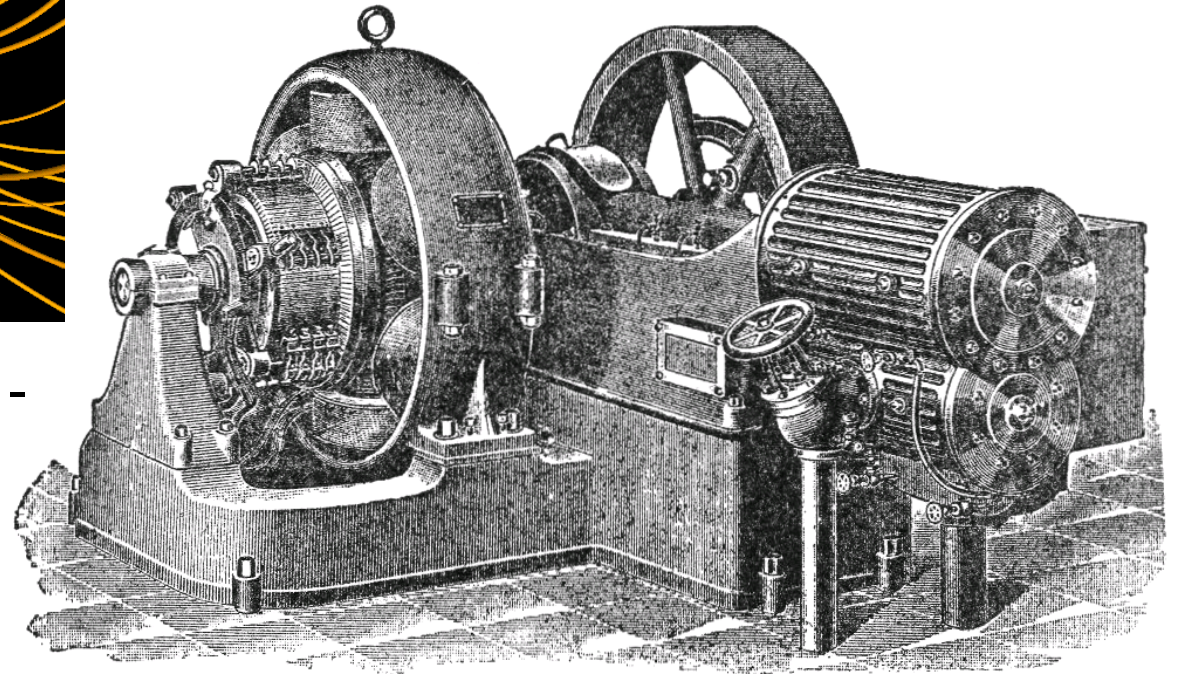
# Dynamos



Reversing Dynamo Simulation -  
Glatzmeier and Roberts



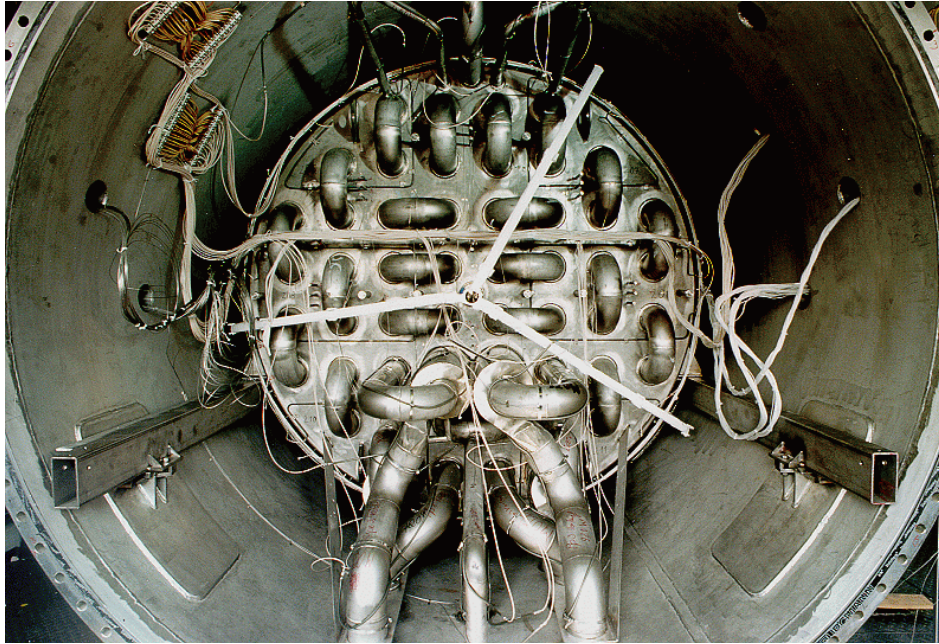
Solar Dynamics - NASA



Looks Like The Plan, But Not The Plan.

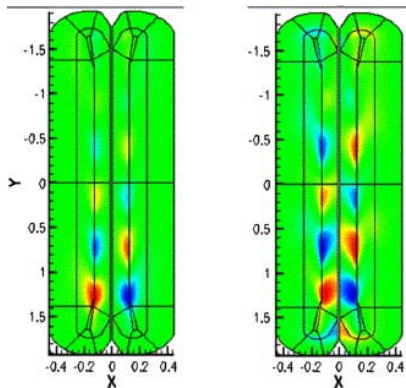
# Dynamos

Important proof that you can build a 'homogeneous' dynamos, or nearly so:  
No electrical insulation, at least!  
Interesting MHD States.

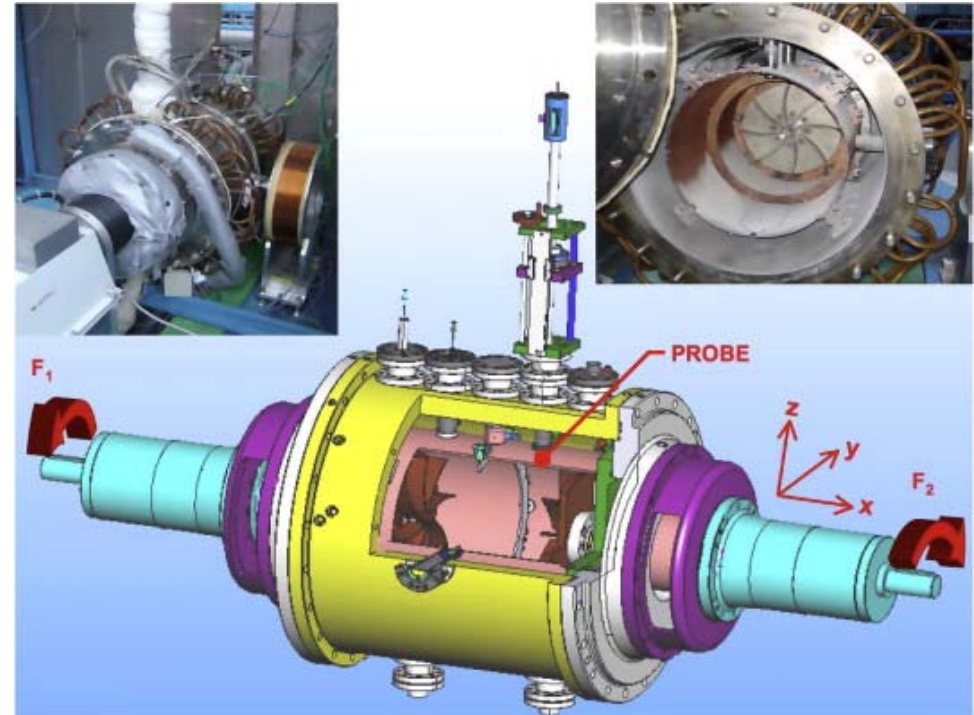
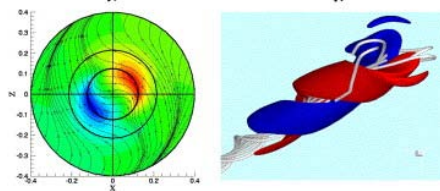


Karlsruhe Dynamo

Constrained Helical Flow Paths



Riga Dynamo-  
Fairly Constrained



Von Karman Sodium II  
Open Geometry but has  
Ferromagnetic Impellers!  
Shows Reversals

Why experiments? - Computer models even further from realistic.

# Dynamos

Planetary and Astrophysically Inspired  
Dynamo Attempts: 3m, Madison Plasma

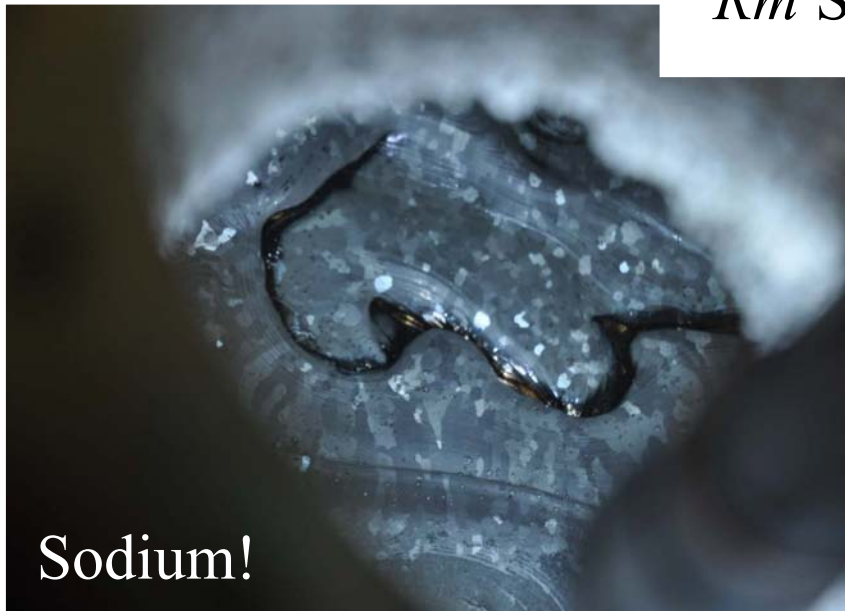
$Re$   
Large



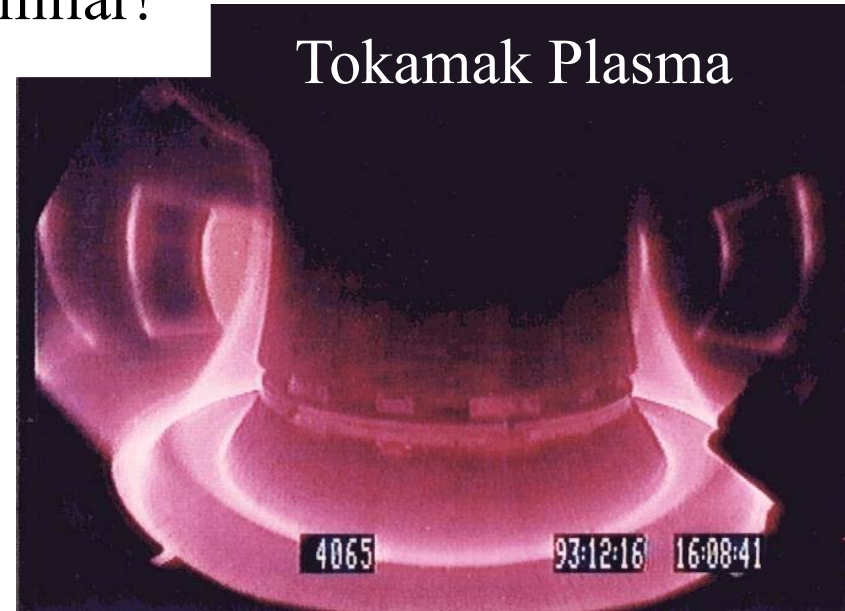
$Re$   
Small

$Rm$  Similar!

$Pm$   
Small



Tokamak Plasma



$Pm$   
Large

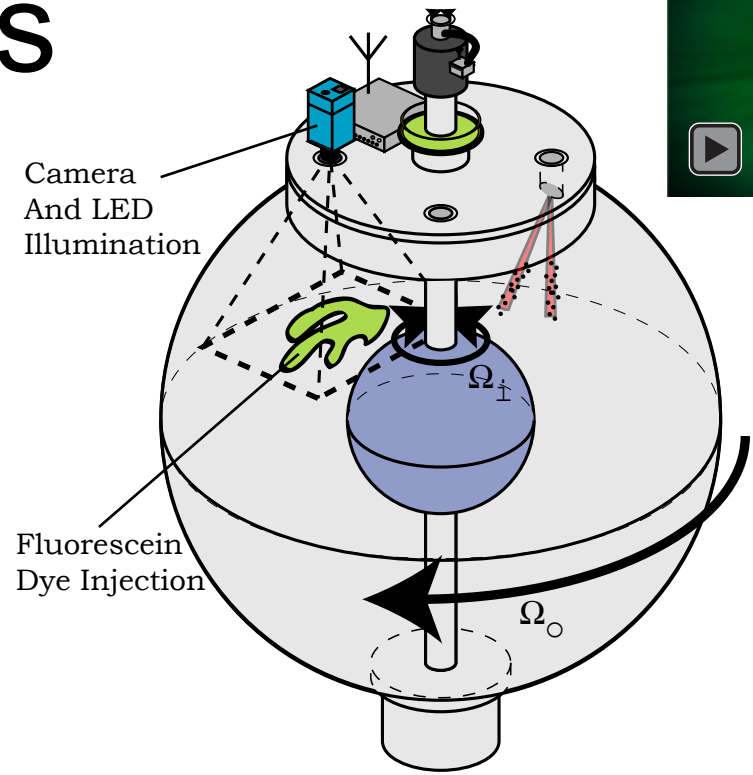
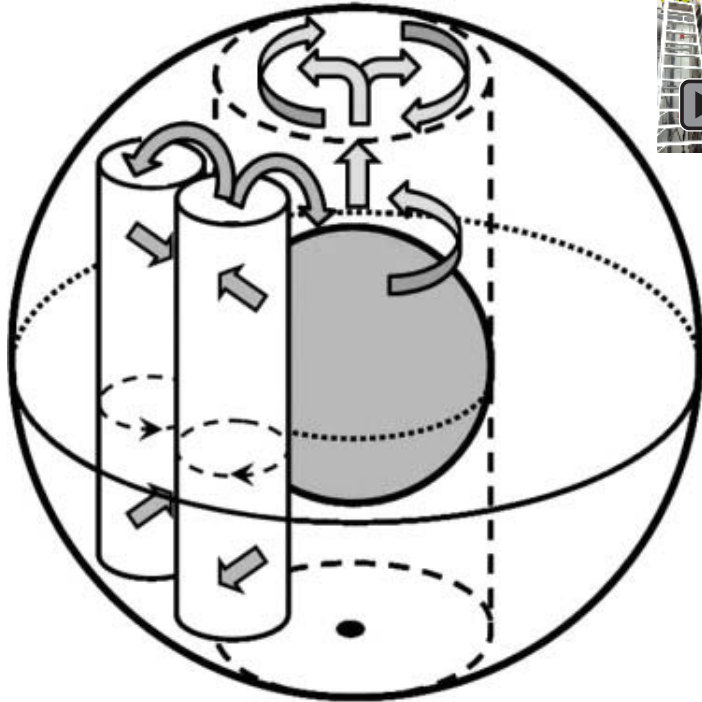
Large  $Re$  = Turbulent!

Large  $Rm$  = Good For Dynamos

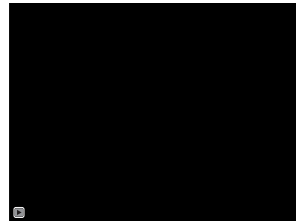
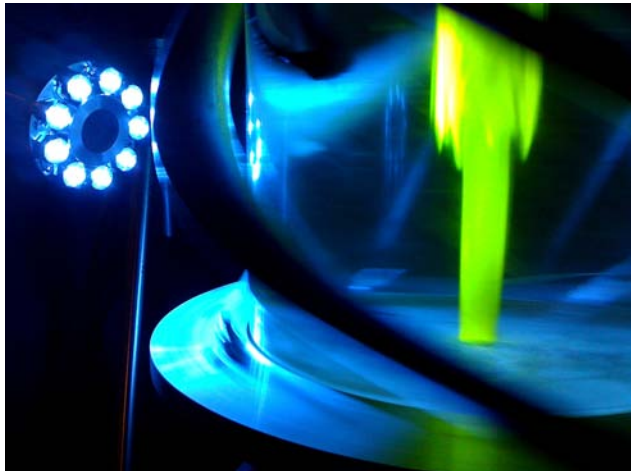
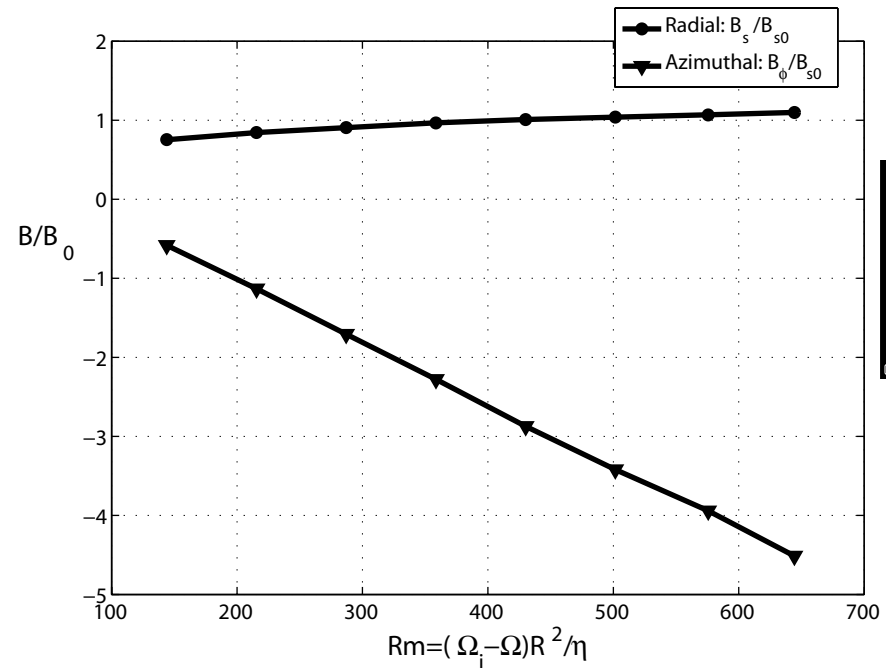
$$Re = \frac{\text{Velocity} \times \text{Size}}{\text{Viscosity}} \quad Rm = \frac{\text{Velocity} \times \text{Size}}{\text{Magnetic Diffusivity}} \quad Pm = Rm/Re = \frac{\text{Viscosity}}{\text{Magnetic Diffusivity}}$$

# Dynamo Ingredients

## Flow Organization From Rotation

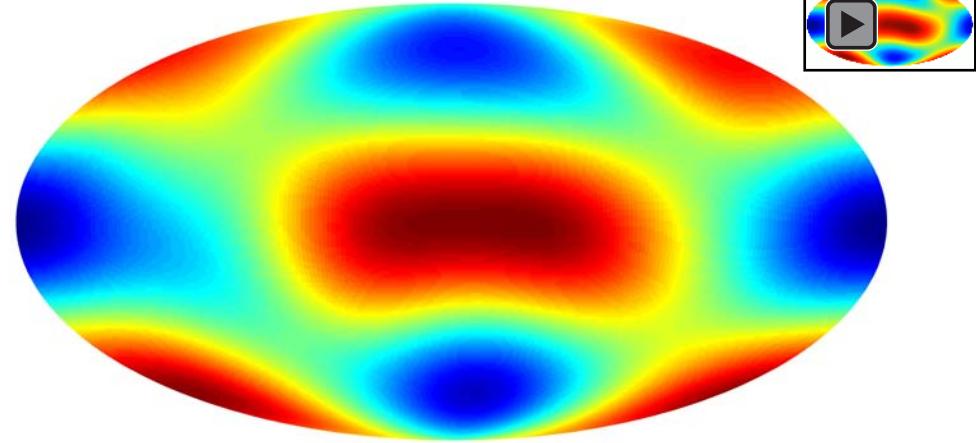


## Winding Up Field Lines: Azimuthal Field vs $Rm$

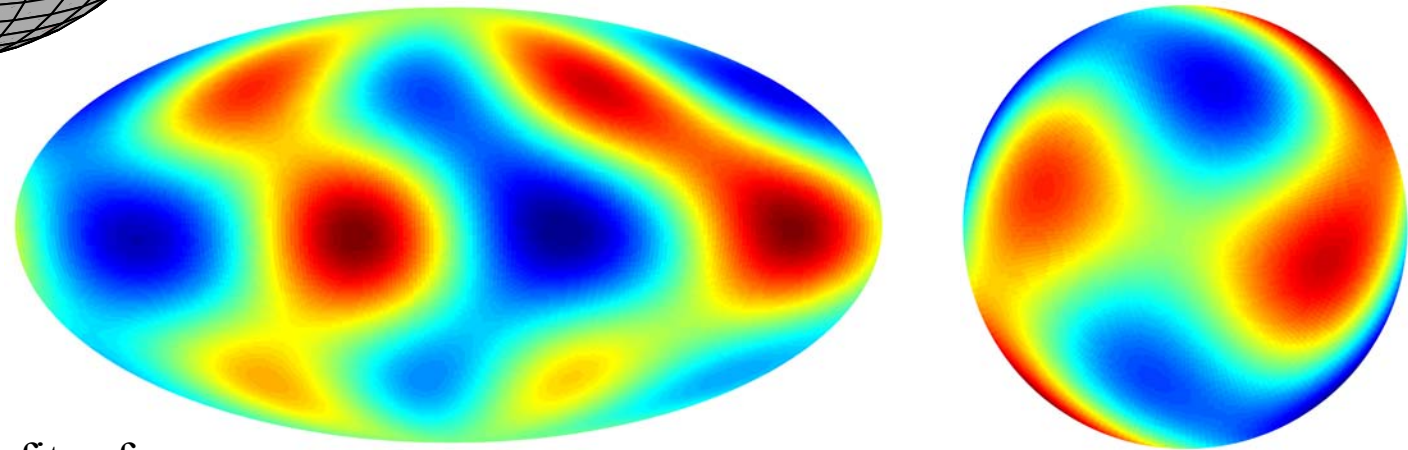


# No Dynamo, But Core-Like Flows!

Weak Magnetic Field - Inertial Mode  
Coriolis Restoring Force



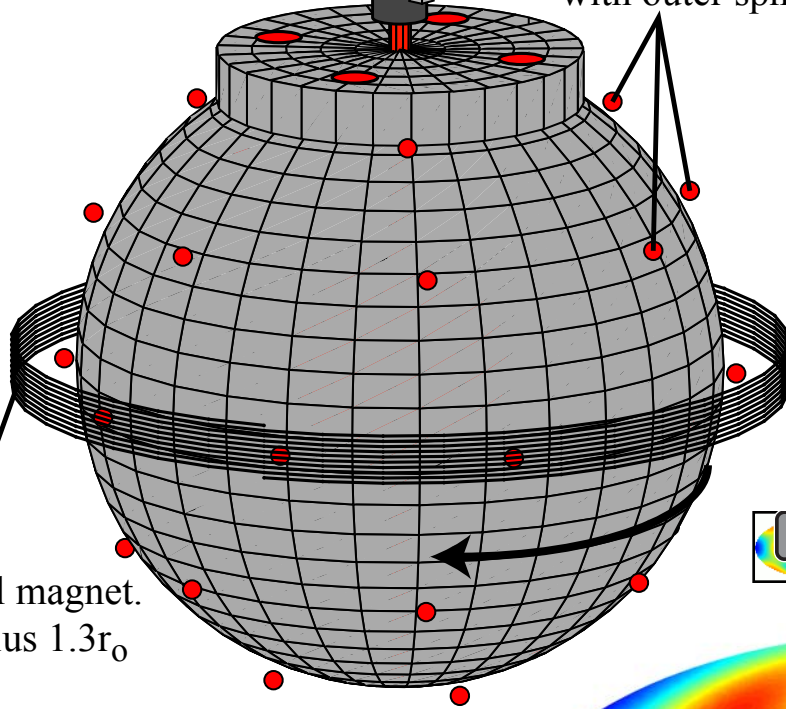
Weak magnetic field - imaging technique!  
Inertial Waves RESPONSIBLE  
for Columnar Flow!



Strong Applied Magnetic Field -  
MAYBE a MagnetoCoriolis (MC) Mode

$\bar{\Omega}, \bar{\Omega}_i$

Hall sensor array.  
31 sensors rotating  
with outer sphere.



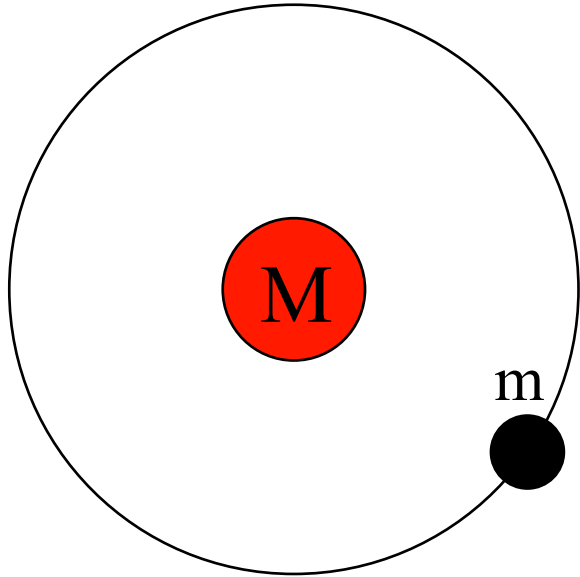
Equatorial magnet.  
Mean radius  $1.3r_0$

Mollweide: Whole  
Sphere Surface Flattened -->

These pictures are least-squares fits of  
spherical harmonic functions to probe data.

# Accretion Disks

Circular orbit,  
angular speed  $\Omega(r)$  in radians/sec



$$m\Omega^2 r = GmM/r^2$$

$$\Omega(r) = \frac{GM}{r^{3/2}}$$

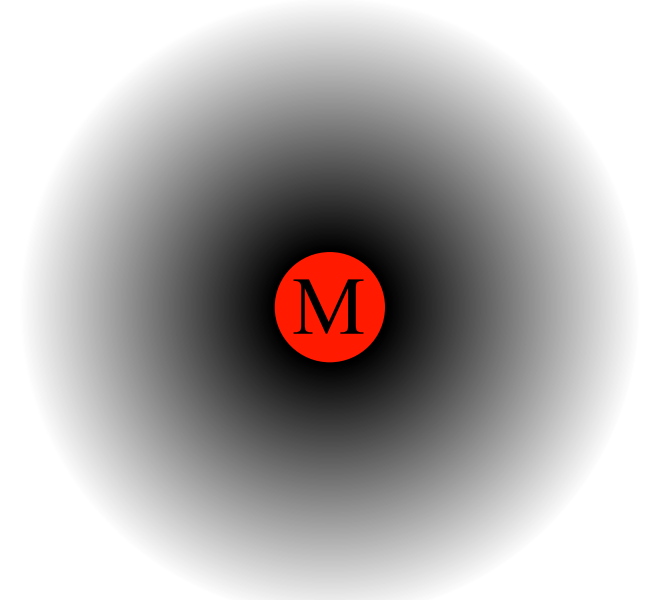
This angular velocity profile may be very STABLE even for enormous Reynolds number (an open question, IMO!)

Why stable? - Inertial Waves!

Why NOT stable? High  $Re$  ( $10^{15}$ !!), Magnetic Field.

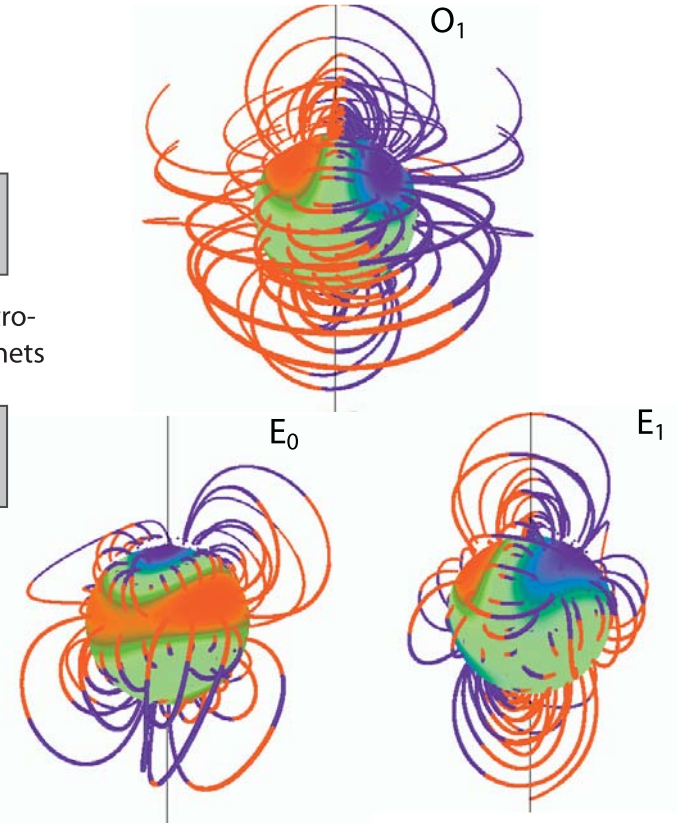
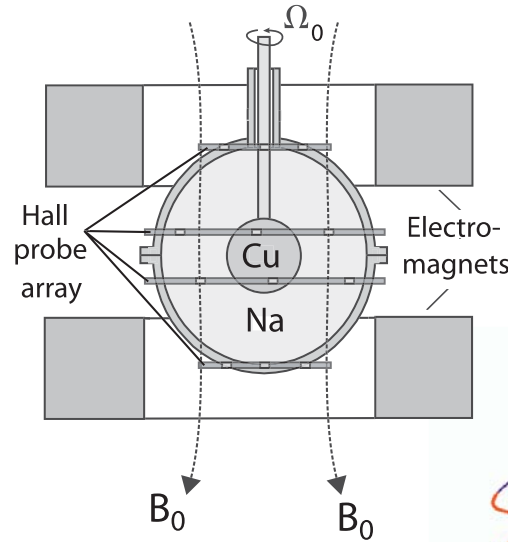
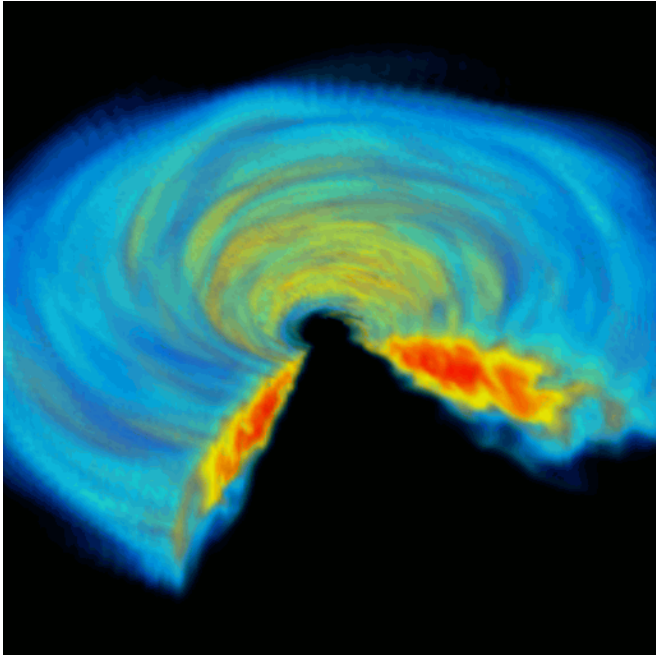
Why does it matter? - Accretion Rate, Angular Momentum Shedding

Orbiting gas and dust  
density  $\rho$   
(when orbiting stuff is colliding)

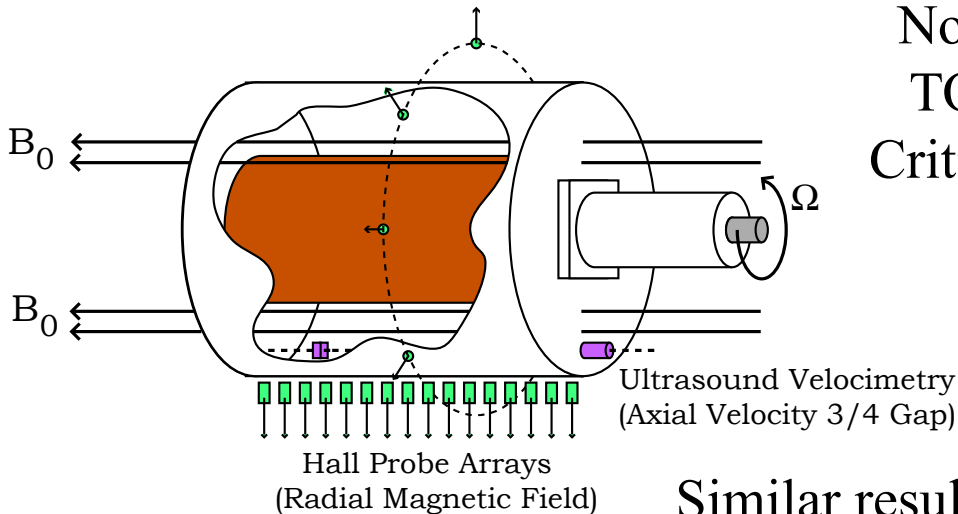


$$\rho\Omega^2 r = G\rho M/r^2$$

# Accretion Disks - MRI



Magnetic Field Changes Stability  
 Allows Overturning Motions,  
 Then Turbulence

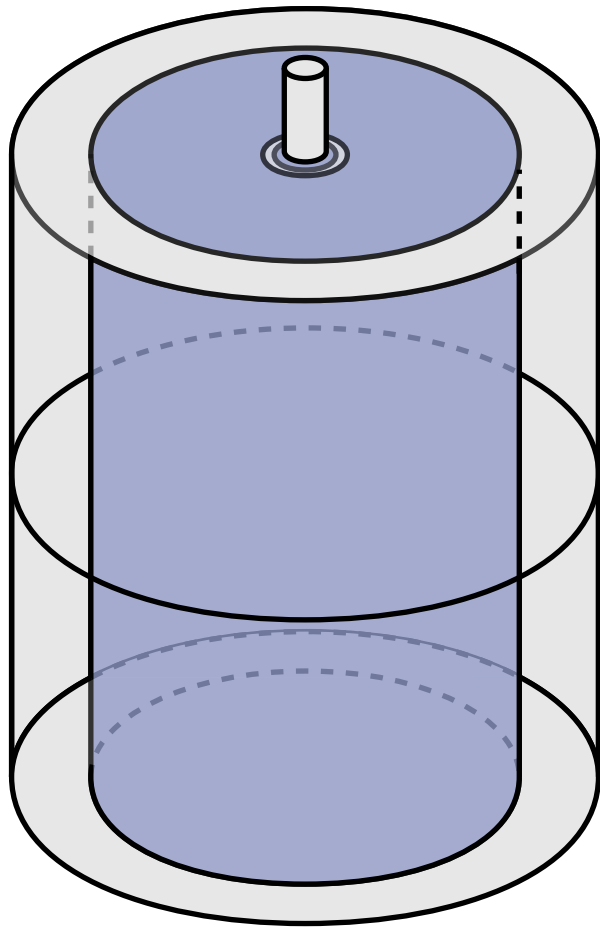


Strong Applied Field - 30cm Experiment,  
 No applied field: flow happens to be  $\Omega \sim r^{3/2}$  !!  
 TORQUE increases  $\rightarrow$  Angular Momentum.  
 Criticism: Already Turbulent. Active research!

Similar results in cylinder.



# Accretion Disks - Hydrodynamics??

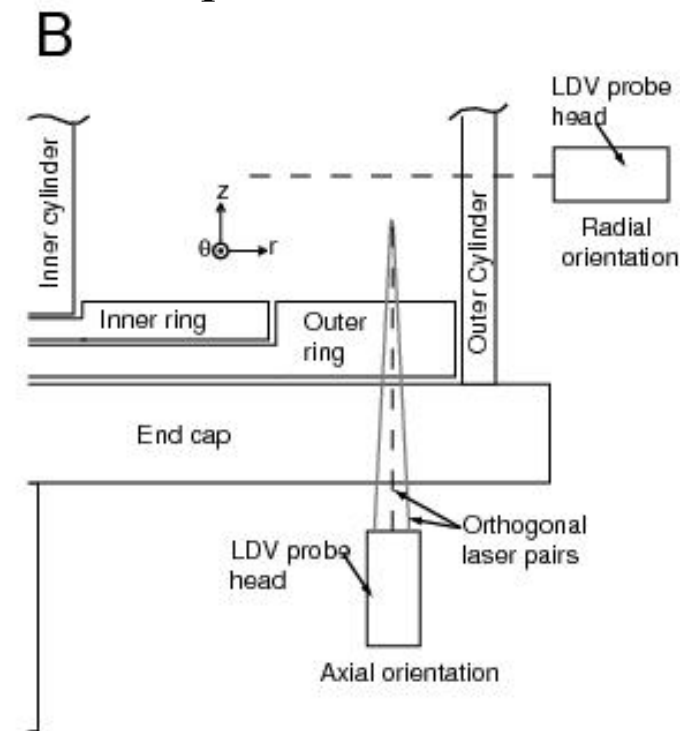
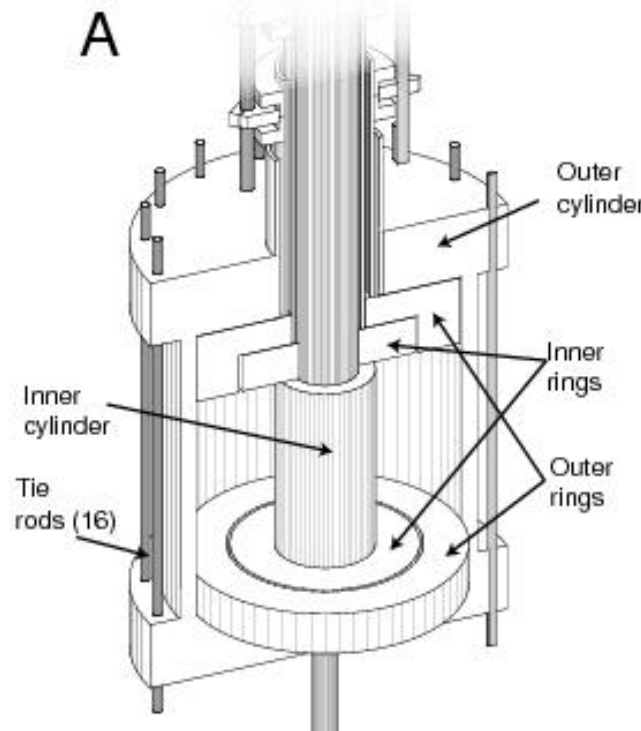


Taylor-Couette  
With BOTH Rotating  
 $\Omega \sim r^{3/2}$  Possible  
Our Experiment is  
Turbulent

Larger  $Re$   
Turbulence from End Effects?

Princeton Apparatus - > Independent  
Inner, Outer, and Two Endwall Rings!  
No Turbulence Reported

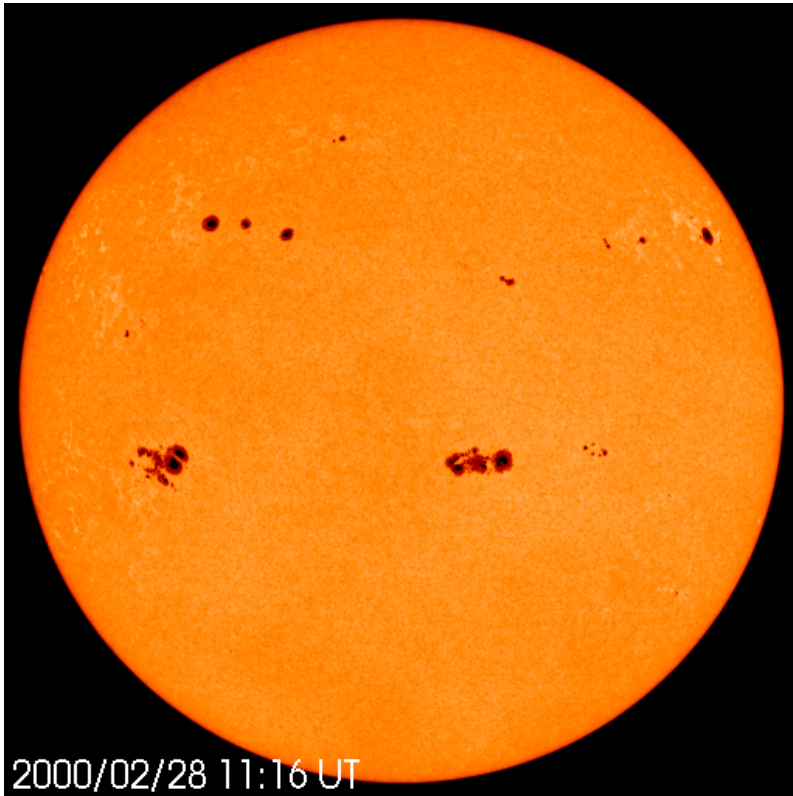
Somewhat Smaller  $Re$   
Rotating ends  $\neq$  No ends  
Measurement Noise 1-2%



Can NEVER be idealized: Need to try many things and find common ground.

# “Helioseismology”

Can't see INSIDE the Sun... Can't see INSIDE sodium, either.

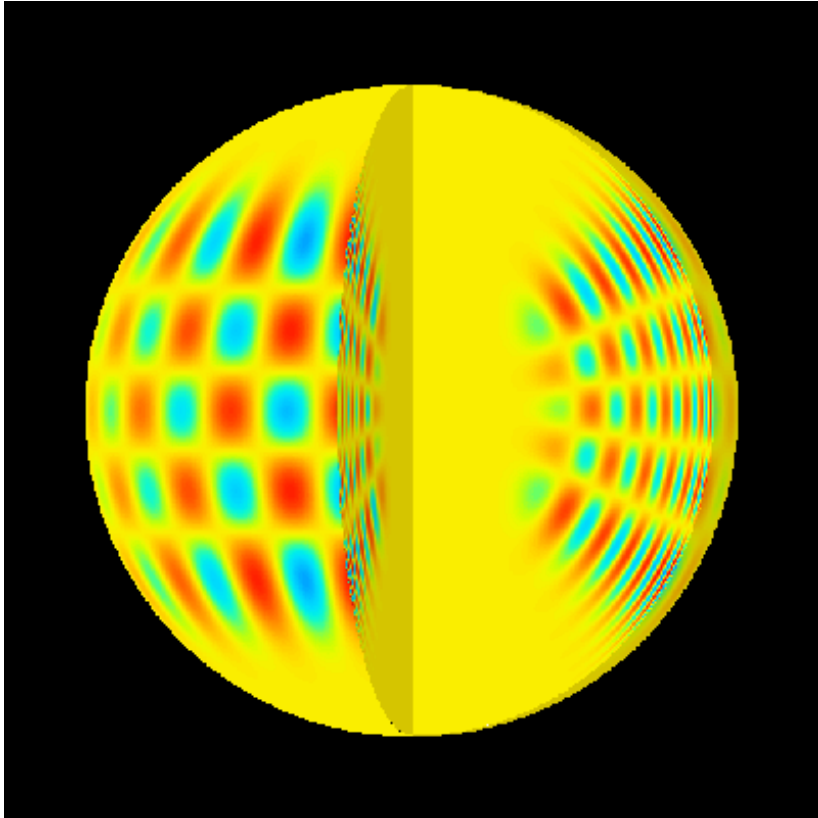


What's the internal flow like??

Ultrasound, but limited to a single pencil beam ... OR...

Thanks to Santiago Triana for some slides...

# “Helioseismology”

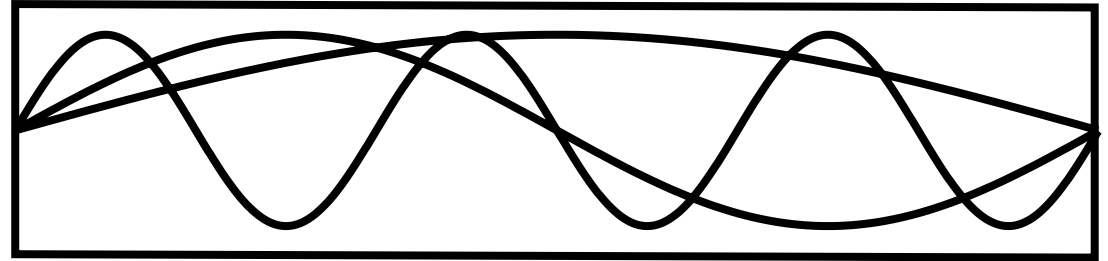


Solar Acoustic Mode

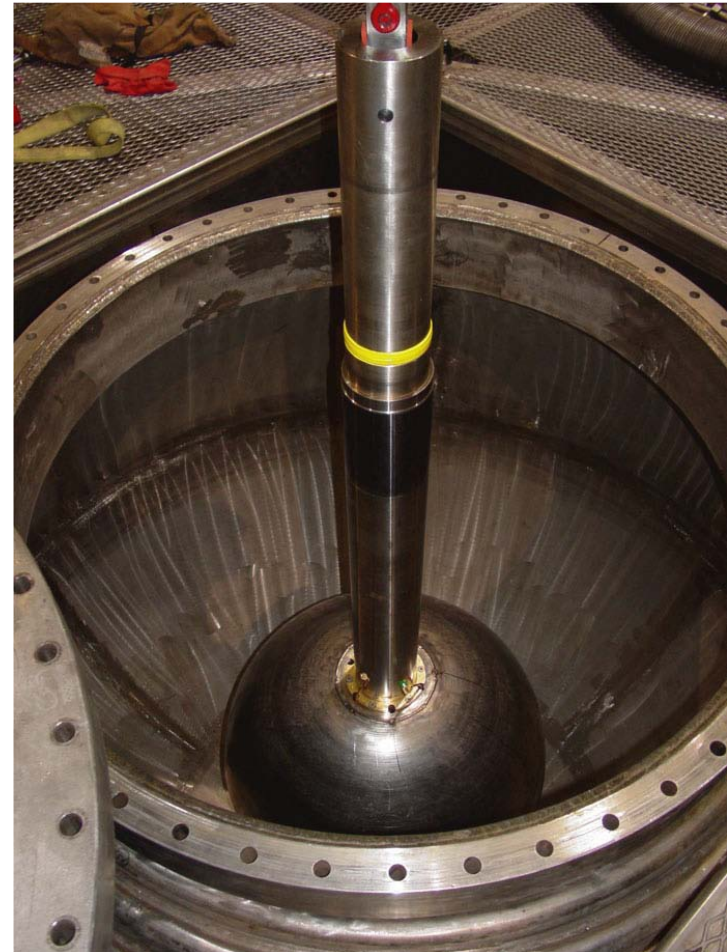
$$\delta\omega = \omega_0 \pm f(\Omega(r, \theta, \phi), \text{mode stuff})$$

System of equations with MANY  $\delta\omega$  for all identifiable modes gives a good guess for rotation profile  $\Omega$

Modes in a Pipe

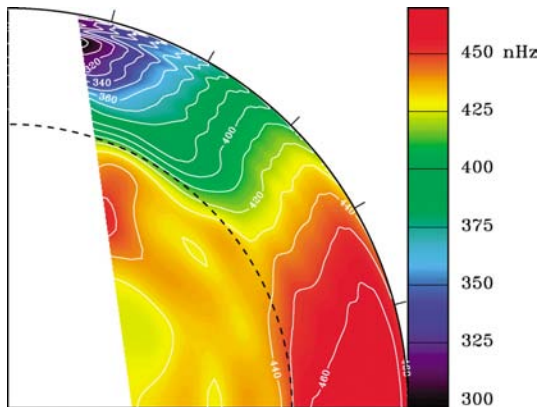


Modes In Here!

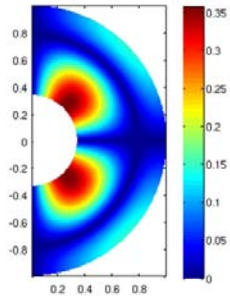


## Acoustic (p-Mode) splitting caused by rotation in the Sun

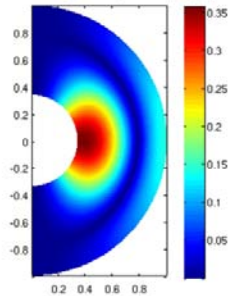
$$\delta\omega_{nlm} = m \int_0^R \int_0^{2\pi} K_{nlm}(r, \theta) \Omega(r, \theta) r \, dr \, d\theta$$



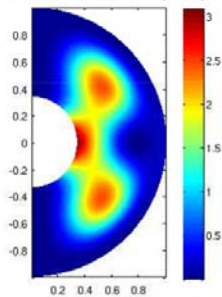
Pressure amplitude, mode (2,2,1)



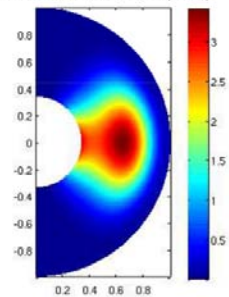
Pressure amplitude, mode (2,2,2)



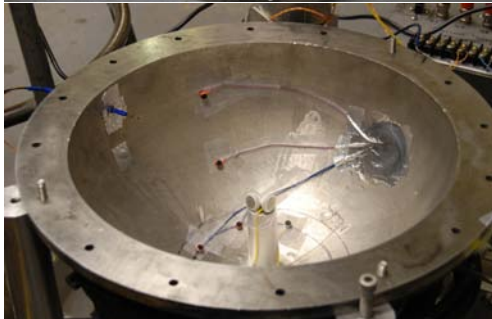
Rotational kernel, mode (2,2,1)



Rotational kernel, mode (2,2,2)



## 30 cm air proof of concept experiment - acoustics easy!



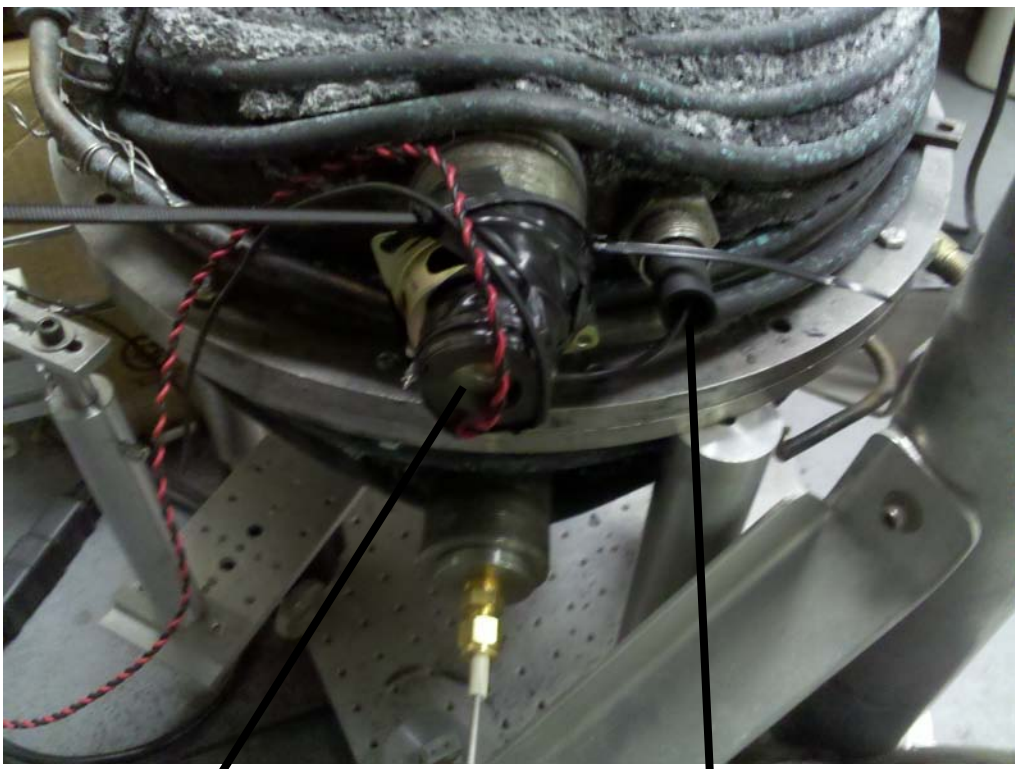
DC motor ~ 5-37Hz:  $12000 < Re < 94000$



TSI Air Velocity Meter

30cm spherical couette  $\eta = 0.33$

Velocity Probe on Transit  
~2.5cm down from equator  
moves in cylindrical radius



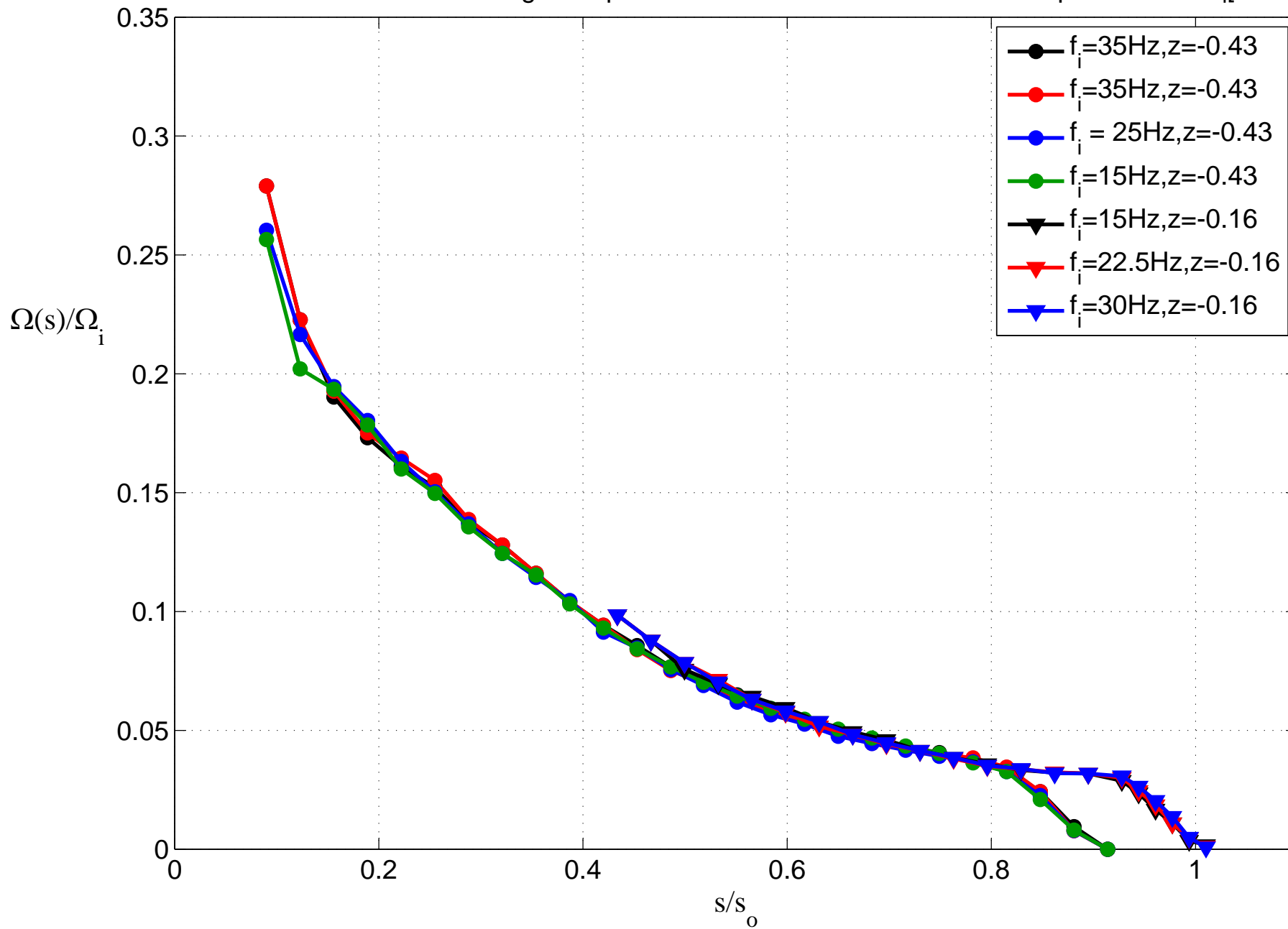
Speaker driven with  
10kHz band limited  
white noise.

Electret microphone

Very lucky find  
hidden in an  
old box:

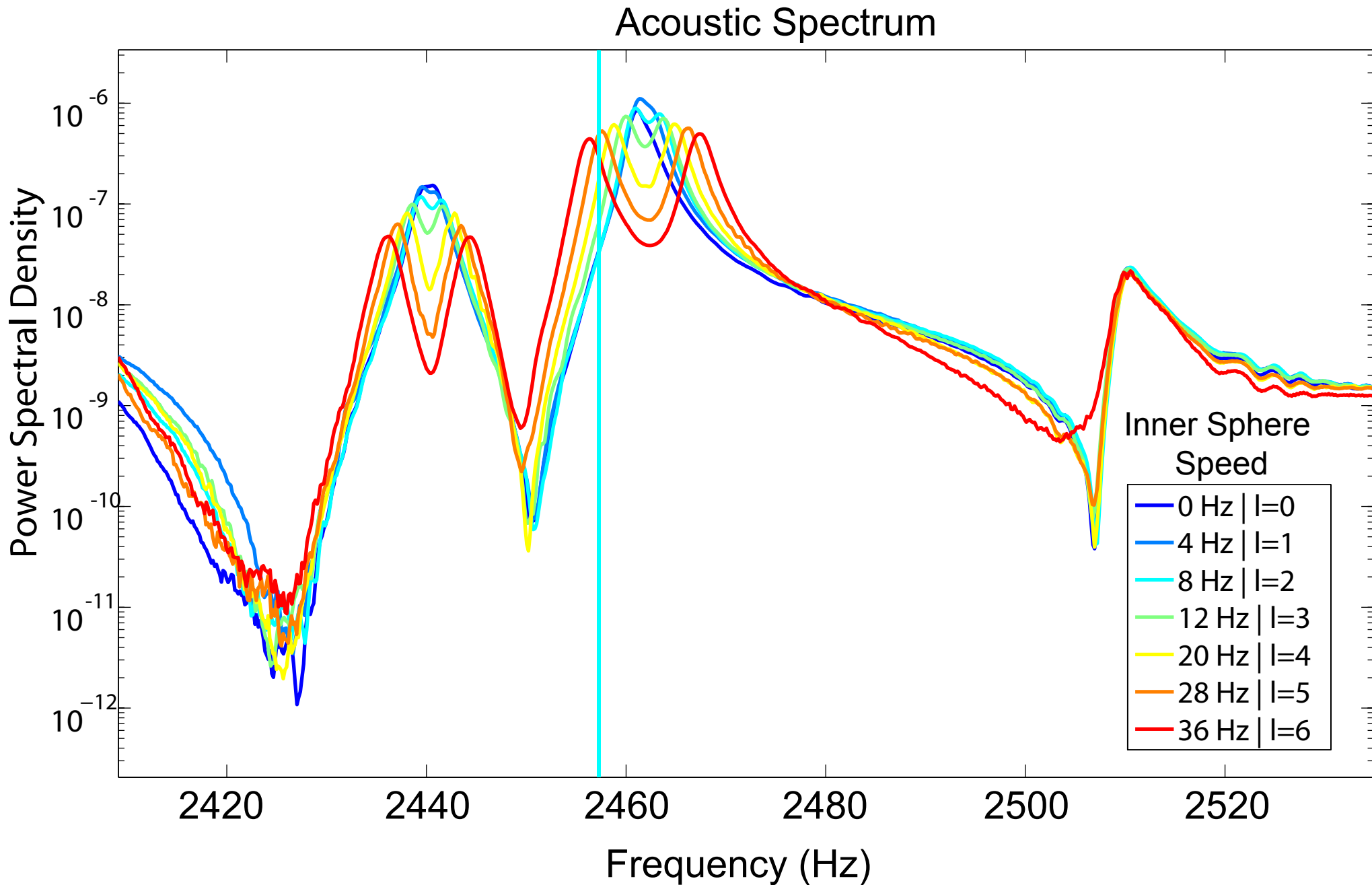


Normalized Angular Speed vs. Radius and Distance from Equator  $\frac{\Omega(s)}{\Omega_i}$  vs  $s/s_o$

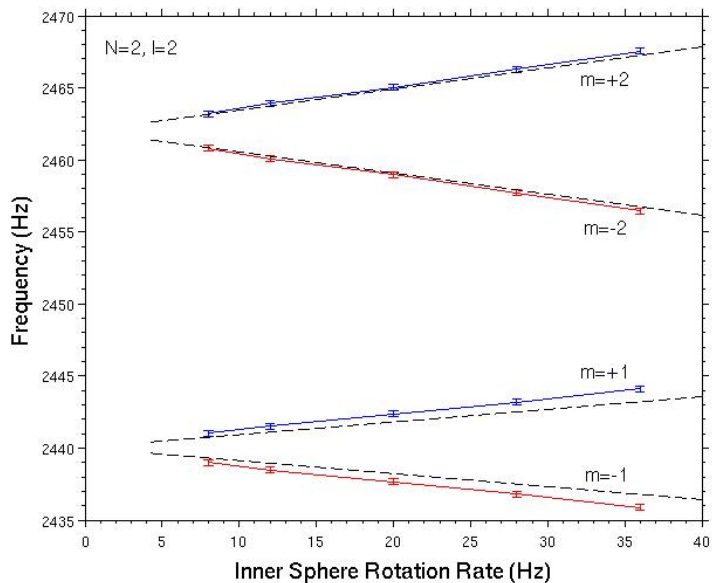




# “Helioseismology”



# Forward problem, splitting is linear with rotation



# “Helioseismology” To-Do

- Need to do the \*inverse\* problem: that’s the useful part.
  - Infer rotation profile from frequency shifts, see if it’s right.
- We have microphones but need a sodium speaker!
- Some promise in “asteroseismology” of distant stars.
  - Instead of full disk measurements, just a point.
  - Inertial modes may be useful here too.
  - Santiago Triana turning into an astronomer (hopefully)